

Key

PETE 301

Exam B

October 27, 2003

(Turn in your 1 cheat sheet with your exam. Show your work. Don't forget the units, if appropriate.)

1. (20 points) A common model for matching relative permeability is the *power curve* which can be expressed in terms of the water saturation,  $S_w$ , and two constants,  $S_{wc}$  and  $S_{or}$ , as follows:  $k_{rw} = \left( \frac{S_w - S_{wc}}{1 - S_{wc} - S_{or}} \right)^3$

Now suppose you have the following lab data:

| $S_w$ | $k_{rw}$ |
|-------|----------|
| 0.31  | 0.008    |
| 0.39  | 0.025    |
| 0.55  | 0.330    |

(a) You want to use a "pseudo straight line". Write the pseudo straight line equation. Indicate the expressions for  $b$  and  $m$ .

$$\sqrt[3]{k_{rw}} = \frac{S_w - S_{wc}}{1 - S_{wc} - S_{or}} = \underbrace{-\frac{S_{wc}}{1 - S_{wc} - S_{or}}}_b + \underbrace{\frac{1}{1 - S_{wc} - S_{or}}}_m S_w$$

$\uparrow$   $y$    $\uparrow$   $x$

(b) What is the independent (x) variable of the pseudo straight-line? Show all three values.

$$x = S_w = \begin{pmatrix} 0.31 \\ 0.39 \\ 0.55 \end{pmatrix}$$

(c) What is the dependent (y) variable of the pseudo straight line? Show all three values.

$$y = \sqrt[3]{k_{rw}} = \begin{pmatrix} 0.2 \\ 0.292 \\ 0.691 \end{pmatrix}$$

(d) Now suppose you have calculated that  $b = -0.41$  and  $m = 2.1$  by linear least squares analysis. From these values, calculate the connate water saturation,  $S_{wc}$  and the residual oil saturation,  $S_{or}$ .

$$m = 2.1 = \frac{1}{1 - S_{wc} - S_{or}}$$

$$b = -0.41 = \frac{-S_{wc}}{1 - S_{wc} - S_{or}}$$

$$S_{wc} = \left( \frac{-S_{wc}}{1 - S_{wc} - S_{or}} \right) / \left( \frac{1}{1 - S_{wc} - S_{or}} \right) = \frac{b}{m} = \frac{-0.41}{2.1} = \boxed{0.195}$$

$$1 - S_{wc} - S_{or} = \frac{1}{2.1} = 1 - 0.195 - S_{or}; \quad S_{or} = 1 - 0.195 - \frac{1}{2.1} = \boxed{0.329}$$

MHJ

2. (20 points) We want to fit the following gas pressure/production data with the straight line material balance equation:  $(p/z) = (p/z)_i [1 - G_p/G]$ . We are not sure of the initial pressure, so we do not want our line to go exactly through the point at  $G_p = 0$ .

(a) In the form of a linear equation,  $y = b + mx$ , what is  $b$ , what is  $m$ ?

$b = \left(\frac{p}{z}\right)_i$        $m = \frac{P_i}{z_i \cdot G}$       - 5

| $G_p$<br>MMscf | $(p/z)$<br>(Bbl/Day) |
|----------------|----------------------|
| 0              | 3000                 |
| 50             | 2755                 |
| 120            | 2410                 |

(b) Use the linear least squares method to calculate the slope and intercept of the straight line. What is the initial gas-in-place,  $G$ ?

$y = b + mx$

$\sum y = nb + m \sum x$       — (1)  
 $\sum xy = b \sum x + m \sum x^2$       — (2)

$$\begin{vmatrix} n & \sum x \\ \sum x & \sum x^2 \end{vmatrix} \begin{vmatrix} b \\ m \end{vmatrix} = \begin{vmatrix} \sum y \\ \sum xy \end{vmatrix}$$

$$b = \frac{\begin{vmatrix} \sum y & \sum x \\ \sum xy & \sum x^2 \end{vmatrix}}{\begin{vmatrix} n & \sum x \\ \sum x & \sum x^2 \end{vmatrix}}$$

$$m = \frac{\begin{vmatrix} n & \sum y \\ \sum x & \sum xy \end{vmatrix}}{\begin{vmatrix} n & \sum x \\ \sum x & \sum x^2 \end{vmatrix}} = \frac{\begin{vmatrix} 3 & 8165 \\ 170 & 426950 \end{vmatrix}}{21800} = \frac{-107200}{21800} = -4.917$$

|                     |
|---------------------|
| $\sum x = 170$      |
| $\sum y = 8165$     |
| $\sum xy = 426,950$ |
| $\sum x^2 = 16,900$ |

$$b = \frac{\begin{vmatrix} 8165 & 170 \\ 426,950 & 16900 \end{vmatrix}}{3(16,900) - 170 + 170} = \frac{65407,000}{21800} = 3000.32$$

$OGIP(G) = \frac{P_i}{z_i m} = \frac{3000}{-4.917} = 610 \text{ MMscf}$       - 3

~~RAW~~ RAW

3. (20 points) Consider the following differential equation describing static pressure in a wellbore:

$$\frac{dp}{dx} = - \left( \frac{2.9 \gamma_g}{z 10.73} \right) \frac{p}{T}$$

where the gas gravity,  $\gamma_g = 0.75$ . A value of  $z = 1.0$  is assumed for simplicity.  $x$  is the vertical distance (positive downward). A temperature gradient of  $1.1^\circ\text{R}/100\text{ ft}$  is assumed to apply. At the surface the wellhead pressure =  $1,500\text{ psia}$  and the temperature is  $90 + 460 = 540^\circ\text{R}$ . Use the Simple Heun method to calculate the temperature and pressure at  $x = 1,000\text{ ft}$ . Use an increment of  $x$  equal to  $1,000\text{ ft}$ . Clearly show your calculations.

Step 1. - Euler method.

$$p_{i+1} = p_i + \frac{2.9 (0.75)}{(1)(10.73)} \frac{1,500}{540} (1000) = 1,500 + (2.0270) \frac{1,500}{540} (1000)$$
$$= 1,500 + 5.63 (1000) = \frac{1,500 + 5,630}{7,130}$$

Step 2. - Heun corrector

$$p'_{i+1} = p_i + \frac{h_i}{2} [f(x_i, y_i) + f(x_{i+1}, y_i)]$$
$$= 1,500 + \frac{1000}{2} \left[ 5.63 + 2.027 \frac{7,130}{(540+11)} \right]$$
$$= 1,500 + 500 [5.63 + 26.23]$$
$$= 1,500 + 500 [31.86]$$
$$= \boxed{17,430}$$

Note: derivative was missing  $\frac{1}{144}$

Answer

4. (20 points) The pressure near the wellbore of a producing well is assumed to correspond to radial flow and can be calculated with the equation  $p(r) = p_{wf} + C \ln(r/r_w)$  where  $C$  is a constant that depends on flow rate, viscosity, permeability, thickness, and wellbore radius ( $r_w$ ). For our case,  $C = 30.5$ ,  $r_w = 0.3$  ft, and  $p_{wf} = 510$  psia at  $r_w$ .

(a) Find the derivative,  $dp/dr$  (from calculus).

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$$\frac{dp}{dr} = \frac{C}{r} = \frac{30.5}{r}$$

(b) Use Euler's method to calculate  $p$  at  $r = 10.3$  ft. Use only one increment ( $h = 10$  ft).

$$p_{i+1} = p_i + \frac{dp}{dr} \Delta r$$
$$= 510 + \frac{30.5}{(0.3)} (10)$$

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$$= 510 + 1016.7$$
$$p(10.3) = \boxed{1526.7}$$

(c) Calculate the difference between this answer with the answer in the  $p(r)$  equation.

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$$p(10.3) = 510 + 30.5 \ln\left(\frac{10.3}{0.3}\right) = \boxed{617.9}$$

(d) What is the best way to improve accuracy?

smaller increments.

difference 
$$\begin{array}{r} 1526.7 \\ - 617.9 \\ \hline \rightarrow \boxed{908.8} \end{array}$$

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MHI

5. (20 points) Indicate the right value of "sum" in the following subroutines.

```
Option Explicit
Sub sumprogram()
Dim n As Integer, sum As Double, i As Integer
sum = 0#
i = 1
Do While (i <= 5)
sum = sum + i
i = i + 1
Loop
End Sub
```

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(a) sum = 15

```
Option Explicit
Sub sumprogram()
Dim n As Integer, sum As Double, i As Integer
sum = 0#
i = 0
Do
sum = sum + i
i = i + 1
Loop While (i <= 5)
End Sub
```

-6

(b) sum = 15

```
Option Explicit
Sub sumprogram()
Dim n As Integer, sum As Double, i As Integer
sum = 0#
For i = 1 To 5
sum = sum + i
Next i
End Sub
```

-6

(c) sum = 15